Two-dimensional crystallization of hard sphere particles at a liquid–liquid interface

Olivier Marnettea, Eric Perez a, Frederic Pincet a, Gary Bryantb,*

a Laboratoire de Physique Statistique de l’Ecole Normale Supérieure, UMR8550 Associée aux Universités Paris VI et Paris VII, 24, rue Lhomond, 75231 Paris Cedex 05, France
b Applied Physics, School of Applied Sciences, RMIT University, Melbourne, Vic 3000, Australia

1. Introduction

Since the initial work over two decades ago [1], interest in the phase behaviour of hard sphere suspensions has increased markedly, with many hundreds of papers published. Colloidal suspensions of hard spheres are excellent model systems for the study of the fundamental processes of crystallization and glass formation. The primary advantage of colloidal suspensions over atomic and molecular systems is that the time scales for crystallization are orders of magnitude slower, and the length scales are orders of magnitude larger, enabling much higher temporal and spatial resolution. Apart from the differences in time and length scales, one of the major differences between crystallization in atomic systems and in colloidal suspensions is that any colloidal suspension contains a range of particle sizes around a mean value—i.e. they are polydisperse. Much of the earlier work largely ignored the effects that polydispersity plays in the phase behaviour of colloidal suspensions. Recently, however, polydispersity effects on colloidal crystallization in three dimensions have attracted attention both in theory and simulation [2–4] and in experimental studies [5–11]. The understanding that has emerged from these studies is that polydispersity has a dramatic effect on the kinetics of phase transitions in three dimensions, as well as on the crystalline structure.

There has also been a considerable amount of interest in phase transitions in 2D systems particularly with regard to nanotechnology applications (e.g. [12,13]). Despite this interest, the effect of polydispersity in two dimensions has received little attention. The only studies to date are: the simulations of Santen and Krauth [14], which suggested the possibility of a 2D glass at high polydispersities; those of Pronk and Frenkel [15], who produced a phase diagram for polydisperse hard disks showing that the miscibility gap does not increase with polydispersity, in contrast to the 3D system; and those of Frydel and Rice [16] which showed that the presence of polydispersity gives rise to an effective interaction. However, to the knowledge of the authors there are no experimental studies of the effects of polydispersity on crystallization in 2D. A number of two-dimensional systems have been studied experimentally, including studies of charged particles trapped at the air/water interface [17], particles with short range paramagnetic repulsions [18–20], and studies of charged particles confined between glass plates [21]. However polydispersity is unlikely to be a significant issue for such systems with ranged interactions. The most extensive experimental studies of quasi two-dimensional systems of hard spheres are those of Rice and colleagues (e.g. [22–25]), using particles confined between glass plates. Despite the elegance and utility of the work using this method, it is not optimal for studying the effects of polydispersity. First, in this system the constraining glass plates have a separation which is ∼20% greater than the particle diameter, meaning that the particles retain a limited degree of vertical motion. Second, there are the complicating effects of the proximity of the confining walls [23,24]. Third, and most importantly, from the perspective of the
current work, if there are particles of different sizes present, the vertical position of their mid-planes may be significantly different, and smaller particles can potentially become trapped above (or below) the mid-planes of the larger ones at high densities.

In this paper we present an experimental approach which is amenable to the study of the effects of polydispersity on the crystallization of hard spheres. The proposed method involves trapping particles at the interface between two immiscible liquids. The principle is that the particles are suspended in the top liquid, and fall under gravity onto the interface with a denser, immiscible liquid below. Even though the particles are denser than the lower liquid, they are trapped at the interface of the two liquids by the interfacial tension. This interfacial tension is sufficiently large that vertical motions due to thermal fluctuations are insignificant compared to the particle size, while lateral motions remain Brownian. The method has in principle several advantages: first, there are no wall effects; second, as there is no possibility of significant vertical motion, the system is much closer to being a true two-dimensional system, which becomes most important for polydisperse and multimodal systems; third, once gravitational settling has occurred the particle density will remain constant if the interface is flat, however if the interface has a small curvature, the system can be slowly compressed (or expanded). This enables the possibility of studying the 2D system during compression. In this paper we describe the system, discuss the difficulties and assumptions, and demonstrate that the particles retain their pseudo hard sphere nature.

2. Materials and methods

The HS particles are made up of polymethylmethacrylate (PMMA), sterically stabilised with polyhydroxy stearic acid (PHSA) and exhibit hard sphere behaviour [26,27] in suitable solvents (e.g. decalin). The particles used here have a mean radius $R$ of 1.36 μm and a polydispersity of 4.9% [5]. In order to develop a method of trapping the particles at a liquid–liquid interface, while retaining their hard sphere character, the liquids must be carefully chosen. Decalin (density 0.89 g cm$^{-3}$, viscosity 2.6 mPa s (20°C)) is chosen for the upper liquid, as this is a standard solvent used for 3D studies of hard spheres, and is well characterized. The lower liquid must be immiscible with decalin, but allow the hard sphere character of the particles to be retained. Ideally the density of the lower liquid should be greater than that of the particles. However, even if the density is slightly smaller, the interfacial tension at the interface may be sufficient to trap the particles. Finally, the second liquid should have a low dielectric constant to minimize the meniscus at the contact line between the particle and the liquids.

The liquid used in this study is 1-3 propanediol (density of 1.05 g cm$^{-3}$, viscosity 39.2 mPa s (20°C)). Although the particle density (1.22 ± 0.03 g cm$^{-3}$) is above the propanediol density, it still allows the particles to be trapped at the interface because of the interfacial tension. The lower density of decalin allows the particles to sediment to the interface. The cell used to anchor particles at the liquid/liquid interface is shown in Fig. 1. The circular cell consists of two sections of different diameter, with a shoulder at a 90° angle to which the interface between the liquids can anchor. Using this approach, the shape of the interface, whether planar, spherical or otherwise, can be controlled with good precision, regardless of the wetting properties of the cell material. Both chambers have an inlet port for injecting the liquids, and the top chamber has an outlet port for air to escape. Thin glass plates are attached to the cell at the top and bottom to seal the cell and allow optical observation.

Prior to an experiment the cell is cleaned by sonication with detergent, rinsed with ultrapure water (18.2 MΩ—Elgastat maxima) and dried. Propanediol (Merck, for synthesis), is injected into the lower chamber with a syringe connected via a flexible tube. Care is taken to avoid air bubbles in the tubes which may be difficult to remove. In general, the surface is curved and it can be made planar by accurately adjusting the volume of injected liquid. Sufficient decalin is then injected through the upper inlet in order to completely fill the cell and remove any air bubbles. The interface is much less visible than the free surface of propanediol, making it impossible to determine the planarity by eye. To roughly check the planarity of the interface, a grid is observed through the cell—if the grid is not deformed, the surface is planar to first order (the planarity is ultimately determined by observing the particles at the interface with the microscope).

Once the interface is approximately planar, both tubes are sealed to fix the volume of the liquids. A small volume of a concentrated suspension of particles is injected through the air outlet using a syringe needle inserted into the middle of the decalin layer, just above the centre of the interface. The air outlet is then sealed, and the system is placed on a microscope stage. Although particles begin to sediment immediately, it takes several hours for all the particles to reach the interface and about 1 day to have a stable distribution of particles at the interface. Assuming the microscope and cell are horizontal, and the liquid volumes have been well adjusted, then one obtains an interface of approximately 30 mm diameter, approximately flat to within ~30 μm. In all cases particles were trapped at the interface, with particles never observed in the lower liquid.

The observation of the two-dimensional hard sphere system is done with a Leica inverted microscope with a magnification of 16×. The focussing is adjusted to have the particles appear as bright spots in the microscope. The centre of the bright spots always has a Gaussian intensity profile. Images from the microscope were recorded with a webcam (1280 × 960 pixels, pixel size 5.6 μm × 5.6 μm, Philips PCVC750K). The images provided by the CCD camera were analysed by detecting local intensity maxima on the bright spots of the image through Gaussian fits using Matlab codes (Matlab 7 and image processing toolbox). More extensive details of the experimental procedure and the analysis can be found in Marnette [28].

The surface fraction occupied by the particles is the parameter which controls the phase behaviour of two-dimensional hard sphere systems. For these experiments it is taken as the number of particles in the field of view multiplied by the mean projected area of a particle, divided by the field of view area. The uncertainty at low magnification is dominated by the number of particles missed by the image analysis and the uncertainty of the mean particle size.

Fig. 1. Schematic of the cell used to confine a hard sphere system in two dimensions. Adjusting the level of the lower liquid allows control of the shape of the interface.
Comparisons between manual and automatic counting lead to an overall uncertainty of about 2% in area fraction.

The simplest measure which can be used to characterize ordering in a two-dimensional hard sphere system is the pair correlation function $g(r)$ which gives the probability of finding a particle at a distance $r$ from a reference particle:

$$g(\|\vec{r}\|) = \frac{\langle dN(r) \rangle}{\rho_o 2\pi dr}$$

where $\rho_o$ is the mean surface density of particles, $\langle dN(r) \rangle$ is the number of particles whose centres are located within a ring of radius $r$ and thickness $dr$, averaged over all the considered particles. The function is obtained from the list of the positions of all the particles at the interface. The list of all the interparticle distances is calculated from one image. Then, the pair correlation function is calculated for interparticle distances $0 < r < r_{\text{max}}$ with a resolution $dr$. $r_{\text{max}}$ is the maximum interparticle separation used in the calculation of $g(r)$. Only the particles which are sufficiently central, i.e. which are located at a distance from the edge larger than $r_{\text{max}}$, can be used to calculate $g(r)$ with their neighbours. For the results presented here $r_{\text{max}} = 25R$, and $dr = 0.05R$. Pair correlations calculated for each central particle are added and normalized to obtain $g(r)$.

3. Results and discussion

Fig. 2 shows images of 2D particles in the fluid phase and the crystalline phase, along with the radial distribution functions, $g(r)$, calculated from each image. While the top image appears to have some local order, this does not correspond to crystallinity, as shown by the $g(r)$, which decays to the noise after around five times the average interparticle distance (indicated by the circles on the image). The bottom image on the other hand shows large crystalline regions, separated by well defined grain boundaries. The observation of grain boundaries is a simple and robust criterion to affirm that a system is in the crystalline state. The size of the crystalline grains is a good indicator of the length of the correlations of crystalline order. This is confirmed by the $g(r)$, which shows that the 2nd peak is split (one of the indicators of crystallinity). This splitting of the second peak will be used hereinafter as the indicator of crystallinity. In addition, the peaks go out to about 20 interparticle distances, which corresponds approximately with the size of the crystals, as indicated by the circle on the image.

Having established that the particles can crystallize on the interface, now it needs to be determined if the hard sphere character of the interactions is maintained. While the interactions cannot be measured directly, the nature of the interactions can be inferred by determining the area fraction at which crystallization is observed, and comparing with the theoretical value.

Fig. 3 shows the $g(r)$ measured at a number of different area fractions between 50% and 80%. The figure on the left demonstrates that long range order begins to appear only above 70%. As shown on the expanded scale on the right, for densities above 72% the second peak shows a clear splitting. Using the position of the first peak as a calibration, the vertical lines show the theoretical peak positions as functions of area fraction. The solid lines indicate the positions of the fluid peaks (at integral values of the first peak), whereas the dotted lines represent the positions of the additional hexagonal crystalline peaks. Theory predicts freezing at an area fraction of 69% and melting at an area fraction of 72.4%. As can be seen in Fig. 3, there is excellent correspondence between the theoretical lines and the crystalline peaks above 75%, while there is no evidence of these
The height of the particle mid-plane relative to the interface is given by [17]:

\[ z = \frac{\gamma_{pl} - \gamma_{pu}}{\gamma_{ul}} R = cR \]

where \( c \) is a constant. The difference in height between the two particles of different size (subscripts L (Large) and S (Small)) would be:

\[ \Delta z = c(R_L - R_S) \]

The individual surface tensions are not known. To estimate the value of \( c \), from the measurements above we assume that 80% of the particle height is in the top liquid, which yields a value of \( c \sim 0.6 \). Note that it may be more appropriate to use the volume or cross-sectional area, but both approximations would yield smaller values of \( c \), and therefore a smaller effect. The value \( c \sim 0.6 \) therefore represents an upper limit of the effect. For the particles used here (\( R = 1.36 \text{ nm} \), polydispersity 4.9%), 95% of particles are between 1.22 and 1.49 \( \mu \text{m} \). For these extremes \( \Delta z \sim 0.16 \mu \text{m} \). This situation is illustrated in Fig. 4 (drawn to scale). As can be seen from the figure, the effective radius of the smaller particle, \( R_{eff} \), is slightly smaller than \( R_S \). From geometry it is easy to show that:

\[ R_{eff} = \sqrt{R_S^2 - \Delta z^2} \]

For the values here this yields \( R_{eff} = 1.21 \) (compared with \( R_S = 1.22 \)). Thus the difference in height is insignificant for polydispersions of order ~5%, and is not very sensitive to the exact value of \( c \).

The final consideration is the contribution of effects which could give rise to behaviour which is not hard sphere in nature, including charging effects and capillary interactions. The particles are sterically stabilised and top liquid is non-polar, so charging effects are expected to be very small. Dipolar effects, if present, would result in a repulsion which would cause crystallization to occur at lower area fractions than is observed here [17]. For particles of similar densities:
size and density, flotation forces lead to an attraction between particles [29]. However, these forces are negligible for particle radii <5–10 \mu m [29]. Moreover, if significant attractions were present, one would expect particles to become trapped in attractive wells, losing their Brownian character. This is not observed here. Thus, while such interactions may exist, they appear to be smaller than the thermal energy, and so do not significantly affect the two-dimensional phase behaviour.

These results show that the system does indeed have behaviour consistent with that of a 2D hard sphere system. There may be deviations from hard sphere behaviour too subtle to be ascertained using the present methods. Other methods for characterizing the interactions, including the use of other criteria for determining crystallinity, such as bond order parameters [25], as well as detailed comparisons with other pseudo 2D hard sphere systems, are left for future work.

Finally, it should be noted that the technique has a number of inherent difficulties. First, optical resolution is low, due to the fact the light passes through multiple interfaces and two layers of liquids, and the particles and liquid have similar refractive indices. In addition, at high densities it is inherently difficult to determine particle positions automatically when they are virtually touching. The use of confocal microscopy combined with fluorescent core particles [30] would significantly improve the resolution. Second, in most experiments there is significant collective drift at all but the highest densities, caused by convective motions in the liquid. This is largely caused by heating due to the illuminating beam, and can be reduced by observing using light filtered through a visible light filter (green). Again confocal microscopy may reduce these effects. Third, obtaining a completely flat interface at the micron level is virtually impossible. However, this also has advantages—the curvature can be used to compress the particles into the centre, or allow them to expand. With careful experiments it may be possible to study the compression and expansion of this system.

4. Conclusions

We have demonstrated an alternative experimental system for studying crystallization of 2D hard spheres. This system confines these spheres at the interface between two liquids chosen to approximately maintain the hard sphere character of the particles. We have shown that the spheres crystallize at approximately the theoretically predicted density, and that the particles undergo two-dimensional Brownian motion. Using this system, studies of the effects of polydispersity on crystallization in 2D may be possible.

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